

formulation', we review the unit commitment problem formulation in the context of day-ahead electricity market, define different DR models, and formulate new UC problems with DR models. Numerical results of these formulations are shown in Section 'Numerical results' while conclusions are given in the final section.

Demand response

(DR) classifications

Different types of demand response have been proposed in the industry. FERC classifies the demand response based on how these programs affect the electricity price and the time frame. Two main categories of DR programs are defined: the incentive-based program and the time-based program. The incentive-based program is further divided into a classical program and the market-based program. Within the classical program, two different approaches have been defined. The first approach is the interruptible/curtailable program where participants receive incentive upfront payments or rate discounts. In this program, participants are asked to reduce their load to predefined values. Otherwise, they will face penalties. The second approach is the direct load control program where some of the participants equipments, such as air conditioners or water heaters, are remotely controlled or possibly shut down by utility or system operator.

The other type of incentive-based program is defined as market-based program. There are four sub-categories in this program: demand bidding, emergency DR, capacity market, and ancillary services market. In the demand bidding program, consumers bid for a specific load that can be reduced. The bid is accepted in market clearing solution if it is less than the market price. Otherwise the customer should curtail the load. In the emergency demand response program, the demand is paid incentives for load reduction during a system emergency. For DR program in capacity market, the load reduction is used to alleviate congestion. Finally, the load curtailment is used to provide reserve in the ancillary services market.

The principal objective of the time-based program is to motivate participants to change the demand values at different time frames in order to flatten the demand curve (aka peak shaving). The electricity price is set to high values for periods when demand reduction is desirable and is set to low values for periods when demand increase is preferable. These price differences are set at different time frames depending on the types of demand response programs: critical peak, extreme day, time of use or real time program.

NERC's demand-side management task force [18] classifies the incentive-based demand response programs into two main categories: the dispatchable controllable demand response (DCDR) and dispatchable economic demand response (DEDR). The first category includes the capacity, ancillary and emergency demand response programs while the demand bid program is included in the second category.

For the purpose of this paper, we can reclassify all available demand response (DRs) into two broad categories: emergency DR and economic DR. Emergency DRs are called and dispatched when system emergency condition requires it to do so. Typically, when the supply situation in the system becomes tighter, then the task of balancing supply and demand can be made easier by calling DRs.

On the other hand, the economic DRs are more voluntary in nature in the sense that the owners of such DRs are willing to reduce or cut their potential demand if they are reasonably compensated by means of favorable price in a market setting or by other means. For example, during a specific market period, if an economic DR owner bid is 30 \$/MW h, and the market clears at 50 \$/MW h, then, that DR will be cleared in that market. In this case, the owner of the DRs be paid 50 \$/MW h (by uniform-pricing rule) for forgoing that demand consumption.

DR programs at RTO/ISOs and utilities

Different RTO/ISOs have different DR programs. The goal here is not to provide detailed analysis of DR programs at RTO/ISOs, but to provide its overview.

For example, PJM operates two main types of demand-related programs: emergency and economic. Emergency Demand Program includes Emergency (capacity and energy) DR Programs and Interruptible Load for Reliability (ILR). Emergency capacity DR is used only in reliability planning study. In Emergency Energy DR program, there are three kinds: annual DR, extended summer DR, and limited DR. Annual DR can be called upon for an unlimited number of times in a delivery year and is required to maintain reduction level for at least a 10 h period. Extended summer DR can be called upon for an unlimited number of times from June through October (extended summer period) and is required to maintain reduction level for at least a 10 h period. Limited DR can be called for a maximum of 10 interruptions per year and has a maximum length of a single interruption of 6 h. Economic demand programs include Price Responsive Demand (PRD), Energy Efficiency Resource, day-ahead DR, and real-time DR Program.

New York ISO (NYISO) operates five demand response programs: Emergency DR program, Special Case Resource program, Targeted Demand Response Program, Day-Ahead DR Program, and Demand Side Ancillary Service Program. California ISO (CAISO) supports three types of DR resources: Non Participating Loads, Participating Loads, and Proxy Demand resources. ERCOT has an emergency interruptible load service program.

In terms of DR programs at utilities, Baltimore Gas and Electric (BGE) offers "Peak Rewards". This DR program is the next generation of Rider 5. BGE offers credits to customers for installing a smart switch or smart thermostat. BGE also employs "smart energy pricing". BGE piloted various dynamic pricing schemes in 2008 and 2009, including a peak-time rebate and critical peak pricing. These pilot programs focused primarily on residential customers and gave them price signals one day in advance of high-priced periods. As an option for the conservation of energy, BGE offers a number of rebates and cost buy-down programs for residential and commercial customers.

Similarly, Sacramento Municipal Utility District (SMUD) in California believed that the smart grid will have a significant impact on SMUD's ability to control loads during peak periods. At Duke Energy in North Carolina, a web-based customer interface directly links the utility-controlled DR to a system in which DR is one of a host of interactive technology solutions for a smarter electric grid.

Unit commitment problem formulation

Unit commitment in a day-ahead market framework

The day-ahead electricity market framework, used in this work, is a simplified market clearing model. This day-ahead market clearing framework only considers transmission system network, generator offers, and fixed load, without or with price-sensitive demand bids (similar to bid-based DRs). The authors understood that the practical day-ahead electricity market also allows participation of additional types of financial instruments, such as virtual bids (incremental offers, decremental bids, and up-to congestion transactions). Modeling these additional components in the day-ahead market clearing framework is beyond the scope of this work. Since our current work is to investigate the impact of DRs on Unit Commitment (UC) and dispatch in the day-ahead market framework, we will focus on the detailed formulation of UC, without or with DRs.

The traditional Unit Commitment (UC) problem [19,20] is formulated as a cost minimization function considering a fixed demand profile without violating any system or unit's operational constraints. The minimization function considers the reduction of generation cost including production cost, start up cost, and no load cost. The UC problem can be expressed mathematically as follows:

$$\min_p \sum_{t=1}^T \sum_{g=1}^G (Cp_{g,t} + Cup_{g,t}) \quad (1)$$

subject to system, unit, and network constraints.

The detailed mathematical formulation for the objective function as well as the constraints included in the simulated model are presented next.

Production cost

Considering the incremental cost function represented by the piecewise function, the production cost function for each unit g at a simulation period t , can be formulated as:

$$Cp_{g,t} = c_g u_{g,t} + \sum_{b=1}^B F_{b,g} \delta_{b,g,t} \quad (2)$$

Additional constraints that need to be added are:

$$p_{g,t} = u_{g,t} P_g + \sum_{b=1}^B \delta_{b,g,t} \quad \forall g, \forall t \quad (3)$$

$$(Tr_{1,g} - P_g) \leq \delta_{1,g,t} \quad \forall g, \forall t \quad (4)$$

$$\delta_{1,g,t} \leq (Tr_{1,g} - P_g) u_{g,t} \quad \forall g, \forall t \quad (5)$$

$$(Tr_{b,g} - Tr_{b-1,g}) \leq \delta_{b,g,t} \quad \forall g, \forall t, b = 2, \dots, B - 1 \quad (6)$$

$$\delta_{b,g,t} \leq (Tr_{b,g} - Tr_{b-1,g}) u_{g,t} \quad \forall g, \forall t, b = 2, \dots, B - 1 \quad (7)$$

$$\delta_{B,g,t} \geq 0 \quad \forall g, \forall t \quad (8)$$

$$\delta_{B,g,t} \leq (\bar{P}_g - Tr_{B-1,g}) u_{g,t} \quad \forall g, \forall t \quad (9)$$

Eq. (2) represents the production costs. Eqs. (3)–(9) are the piecewise linearization of production costs. Fig. 1 illustrates the different variables used for this formulation.

Start up cost

For the start up cost model, a discretized exponential model can be used. Based on the discretized approximation, a simple mathematical formulation for the start up cost is included per unit g and per simulation period t :

$$Cup_{g,t} \geq K_{\tau,g} \left(u_{g,t} - \sum_{n=1}^{\tau} u_{g,t-n} \right) \quad \forall g, \forall t \quad (10)$$

System constraints

The system restrictions include the power balance equation and the reserve constraints

$$D_t - \sum_{g=1}^G p_{g,t} = 0 \quad (11)$$

$$R_t + D_t - \sum_{g=1}^G r_{g,t} \leq 0 \quad (12)$$

Minimum on/off conditions

These restrictions can be formulated as follows [21]:

$$\sum_{i=t-MU_g+1}^t s_{g,i} \leq u_{g,t} \quad \forall g, \forall t \in [MU_g + 1, T] \quad (13)$$

$$\sum_{i=t-MD_g+1}^t h_{g,i} \leq 1 - u_{g,t} \quad \forall g, \forall t \in [MD_g + 1, T]$$

For the initial period, the number of periods that the unit is on or off need to be considered:

$$\sum_{i=0}^{i \leq T_g^{on}} 1 - u_{g,i} = 0 \quad \forall g, t = 0$$

$$\sum_{i=0}^{i \leq T_g^{off}} u_{g,i} = 0 \quad \forall g, t = 0 \quad (14)$$

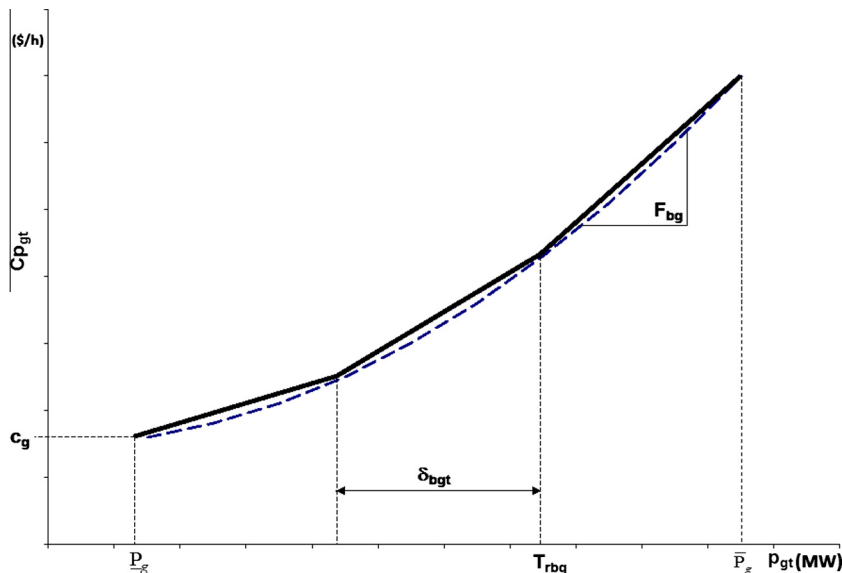


Fig. 1. Linear production cost curve.

Ramp up and down constraints

$$\begin{aligned} p_{g,t} - p_{g,t-1} &\leq RUL_g \quad \forall g, \forall t \geq 0 \\ p_{g,t-1} - p_{g,t} &\leq RDL_g \quad \forall g, \forall t \geq 0 \end{aligned} \quad (15)$$

Network constraints are included using Bender's Cuts, this formulation is explained in the next section.

Benders cut constraint

The coupling between the UC problem and the network sub-problems is done through the economic dispatch variable \mathbf{P}^* , which is the solution of problem shown in Eqs. (1)–(15). The sub-problem can be formulated as:

$$w^* = \min(\mathbf{c}_x \cdot \mathbf{x}^i) \quad (16)$$

subject to:

$$\left. \begin{aligned} \mathbf{Y}_s^i \theta^i &= \mathbf{P}^i - \mathbf{D} & \pi_D \\ -\bar{\mathbf{f}}^i &\leq \mathbf{f}^i + \mathbf{z}^i \leq \bar{\mathbf{f}}^i & \pi_f \\ \underline{P}_i &\leq \mathbf{P}^i \leq \bar{P}_i & \pi_p \\ |\mathbf{P}^i - \mathbf{P}^0| + \mathbf{x}^i &\leq \Delta^i & \pi_\Delta \end{aligned} \right\} \text{constraints for network scenario } i \in [0, \Omega_{NC}] \quad (17)$$

In this case, the Benders Cut is created for each network scenario:

$$w^* + \pi_\Delta \cdot (\mathbf{P} - \mathbf{P}^*) \leq 0 \quad (18)$$

A more detailed explanation of how the network constrains are included into the problem using Benders decomposition can be found in [22–24].

Demand response models

In the UC formulation described in the previous section, the demand is considered as a fixed value. However, in order to consider the effect of the demand response, a variable demand as a function of the bid needs to be modeled. One logical alternative is to model that bid-dependent demand as shown in Fig. 2. Each price-sensitive demand can submit multiple non-incremental demand bid blocks as shown in the same figure. Note that the demand bids are represented by downward-sloping curves.

Mathematically, the demand bid value function can be defined by:

$$DB_{j,t}(d_{j,t}) = \sum_{k=1}^{\Omega_{b,j,t}} CB_{k,j,t} \cdot Bid_{k,j,t} \quad \forall j, \forall t \quad (19)$$

where

$$\sum_{k=1}^{\Omega_{b,j,t}} Bid_{k,j,t} = d_{j,t} \quad \forall j, \forall t \quad (20)$$

and

$$Bid_{k,j,t} \leq MWB_{k,j,t} \quad \forall j, \forall k, \forall t \quad (21)$$

New unit commitment problem with DR models

In this new UC problem formulation, the price sensitive demand can be introduced into the minimization objective function as follows:

$$\min \sum_t \left[\sum_{g=1}^G (Cp_{g,t} + Cup_{g,t}) - \sum_j DB_{j,t}(d_{j,t}) \cdot dU_{j,t} \right] \quad (22)$$

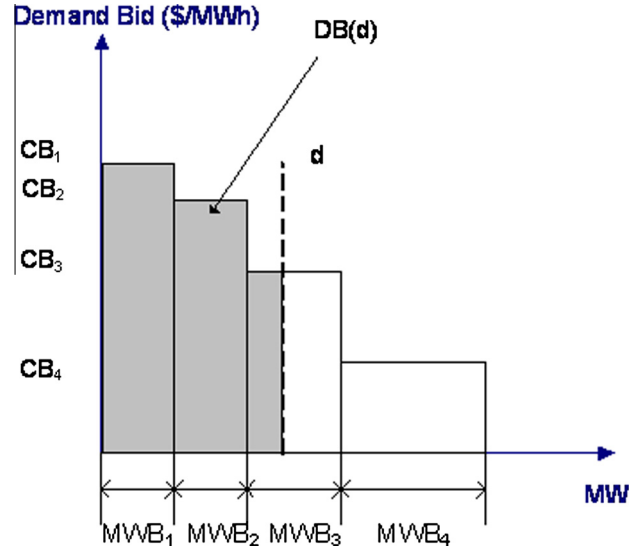


Fig. 2. Price sensitive demand bid blocks.

The additional constraints due to the demand model are:

$$D_{j,t}^{\min} \cdot dU_{j,t} \leq d_{j,t} \leq D_{j,t}^{\max} \cdot dU_{j,t} \quad \forall j, t \quad (23)$$

$$dU_{j,t} = 0 \quad (\text{or}) \quad 1 \quad \forall j, t \quad (24)$$

$$dU_{j,t} = \begin{cases} 0 & \text{if demand resource } j \text{ is off at period } t \\ 1 & \text{if demand resource } j \text{ is on at period } t \end{cases} \quad (25)$$

The system constraint must also be modified as:

$$\left[D_t + \sum_j d_{j,t} - \sum_{g=1}^G p_{g,t} \right] = 0 \quad \forall t \quad (26)$$

Numerical results

The main objective of this work is to simulate and evaluate the impact of DR on unit commitment, generation dispatch, and resultant LMPs based on the formulation previously described. The IEEE 118 bus test system [17] is used to study the problem. Additional input data into the UC problem such as the generator bids and the hourly load profiles are described in Appendix A. The model is implemented in GAMS using CPLEX as the solver, with all the parameter options set to the default values.

We classify the study cases into two main categories: without network constraints and with network constraints.

Without network constraints

First, the system with fixed load, but without any DR resources, is simulated without any network constraints for a 24 h simulation time frame. The hourly marginal prices, also known as market prices (MP) or LMP, are calculated. These results are compared with those of the same system with a DR resource bid of 9 \$/MW h (arbitrarily chosen) up to 500 MW from hour 12 to hour 24. The comparisons of MPs for the two cases are illustrated in Fig. 3.

The load forecast described in the Appendix illustrates that this load was larger than the demand max bid of 500 MW, for periods 19 and 20. Therefore, this specific load for those periods was reduced to 500 MW with DR bids, thus, reducing the market prices (\$/MW) accordingly. However, there was also a scheduling impact

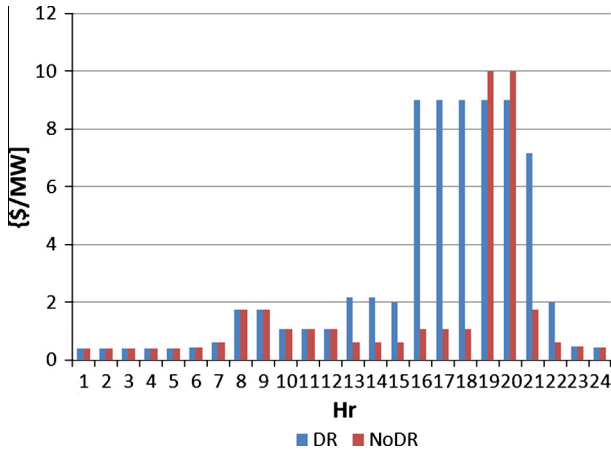


Fig. 3. Resultant MPs for cases with and without DR bids.

for the other hours. Due to such differences in generator scheduling, the MPs can increase in other periods as can be seen from periods 13 through 18, as well as in periods 21 and 22. Regardless of price variations, the total costs of production are reduced from the simulation case without DR resource (4312.3) to the simulation case with DR resource (1152.9). Note the significant reduction of production cost in the case with DR resource.

For the case with DR resource bid, the DR bid MWs were also increased to observe the evolution of market prices. Fig. 4 shows the comparison of results for four different DR bid MW values: 500 MW, 1000 MW, 1500 MW, and 2000 MW, denoted by DR500, DR1000, DR1500, and DR2000 respectively in the same figure.

Results show that the market prices were reduced by modeling and incorporation of the demand response in the market clearing problem formulation. However, some price spikes can be observed when the values of DR MWs were increased due to the non-convexity of the unit commitment problem. Therefore, it is recommended that this type of impact should be considered and evaluated before such a DR program is incorporated into any relevant unit commitment and dispatch problem in an electricity market environment. The authors also believe that different power systems would behave differently with the inclusion of different amount of DR resources.

With network constraints

In addition to previous cases (without and with DRs) without network constraints, simulations were also carried out for a system including network constraints. Since the branches in the test system have no thermal limits, some reasonable limits were added for these branches in order to make the system suitable for the SCUC simulation, considering some network binding constraints. For that reason, the limit for a branch from bus 30 (Sorenson) to

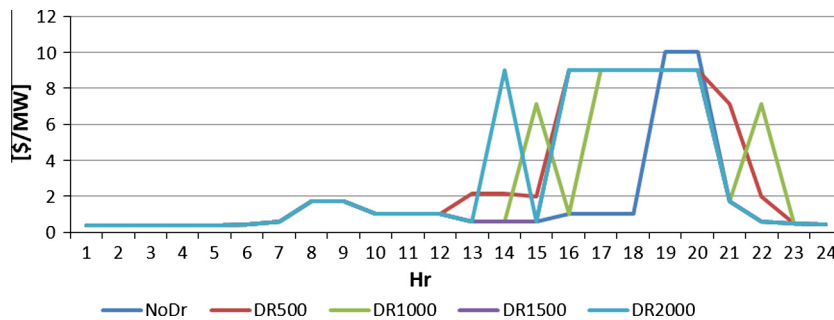


Fig. 4. Hourly LMP differences for cases with different DR bid MWs.

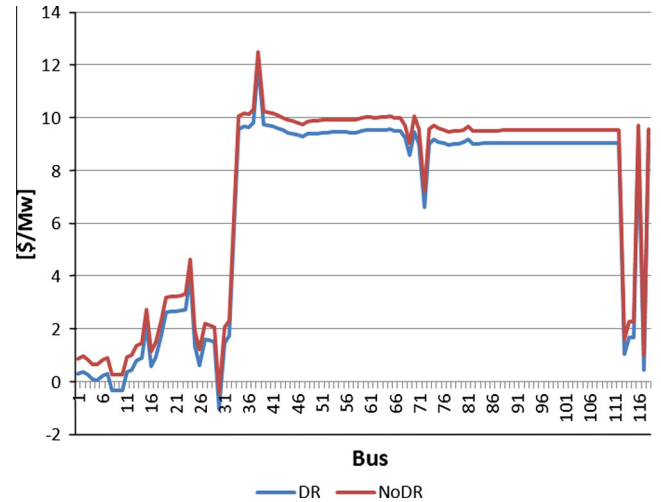


Fig. 5. Bus LMP differences for cases with network congestion at hour 16.

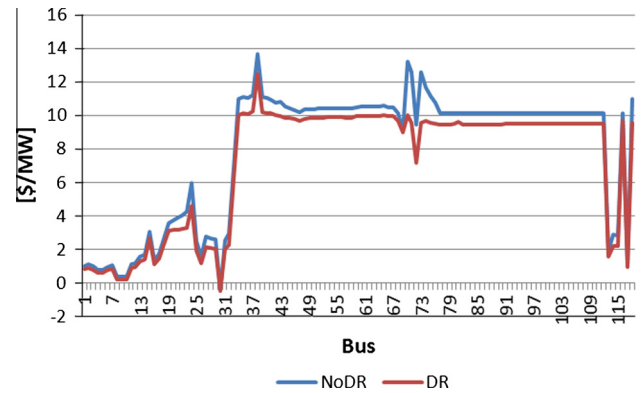


Fig. 6. Bus LMP differences for cases with network congestion at hour 18.

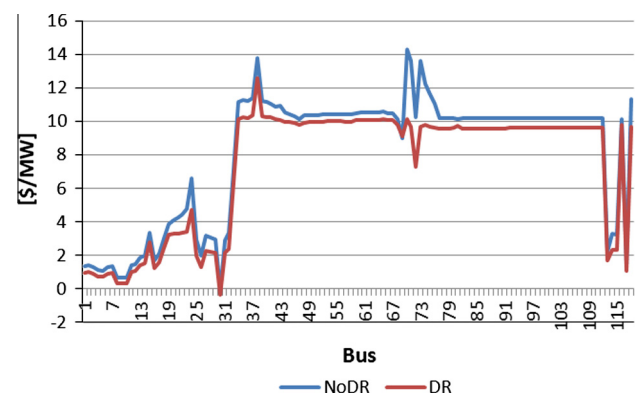


Fig. 7. Bus LMP differences for cases with network congestion at hour 19.

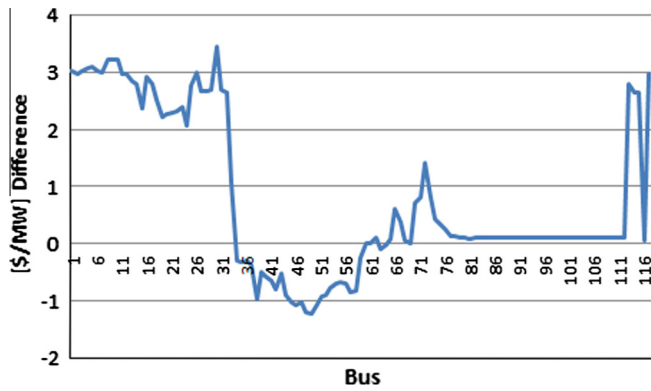


Fig. 8. Bus LMP differences between cases of NoDR and Load Response at hour 19.

Table A.1
Hourly LMP differences [\$/MWh].

Period [h]	No Bid	500 MW	1000 MW	1500 MW	2000 MW
13	0.61	2.17	0.61	0.61	0.61
14	0.61	2.17	0.61	0.61	9
15	0.61	2	7.14	0.61	0.61
16	1.05	9	1.05	9	9
17	1.05	9	9	9	9
18	1.05	9	9	9	9
19	10	9	9	9	9
20	10	9	9	9	9
21	1.72	7.14	1.72	1.72	1.72
22	0.61	2	7.14	0.61	0.61
23	0.47	0.47	0.47	0.47	0.47
24	0.43	0.43	0.43	0.43	0.43

bus 38 (EastLima) was set to 83 MVA, the limit for a branch from bus 9 (Bequine) to bus 10 (Breed) was set to 460 MVA, and the limit for a branch from bus 49 (Philo) to bus 66 (Musknugum) was set to 132 MVA respectively. Figs. 5–7 show the comparisons of bus MPs for the cases with and without DR bids, for three different hours (hour 16, 18, and 19). The DR bids for this case were set to have the same values as in the previous case without network constraints.

Fig. 8 illustrates the price difference at each bus, for hour 19, between the case without DR (NoDR) and the case with load response. The load response was modeled as component of the load that can be scheduled to shut down. The cost of that shut down was modeled as \$1 for shutting down 100 MW of load at any instant. Note that in this case, although the total cost is reduced, due to the network constraints, LMPs at some buses may increase. We included the same network limits in this case, as in previous cases.

From these results, it can be concluded that the DR resources which are distributed at different load buses, can also have a positive impact in alleviating the network congestion, as well as the reduction of the LMPs at different buses. Table A.1 provides hourly LMP differences between basecase and those cases with DRs. Table A.2 also shows the cost reduction as a percent of the basecase results due to the increase in MW of the demand bid.

Conclusion

Demand response (DR) resources are going to play a more important role in the operation of power systems and electricity market in the near future. Their participations in the electricity market are going to have a significant impact on market outcome by impacting the security-constrained unit commitment and

Table A.2
Cost reduction (in percentage) due to demand bid.

Demand bid (% w.r.t base demand)	UC total cost reduction (%)	SUCU total cost reduction (%)
1.25	3	3
2.50	2.3	2
3.75	3.2	3
5.00	4.5	3.5
7.50	7.3	6
10.00	10	7
12.50	14	7.5

Table A.3
Generator offers.

Bus	Bid (\$/MWh)	Bus	Bid (\$/MWh)	Bus	Bid (\$/MWh)
1	10	49	0.47	90	10
4	10	54	1.72	91	10
6	10	55	10	92	10
8	10	56	10	99	10
10	0.22	59	0.61	100	0.38
12	1.05	61	0.59	103	2
15	10	62	10	104	10
18	10	65	0.25	105	10
19	10	66	0.25	107	10
24	10	69	0.19	110	10
25	0.43	70	10	111	2.17
26	0.31	72	10	112	10
27	10	73	10	113	10
31	5.88	74	10	116	10
32	10	76	10		
34	10	77	10		
36	10	80	0.21		
40	10	85	10		
42	10	87	7.14		
46	3.45	89	0.16		

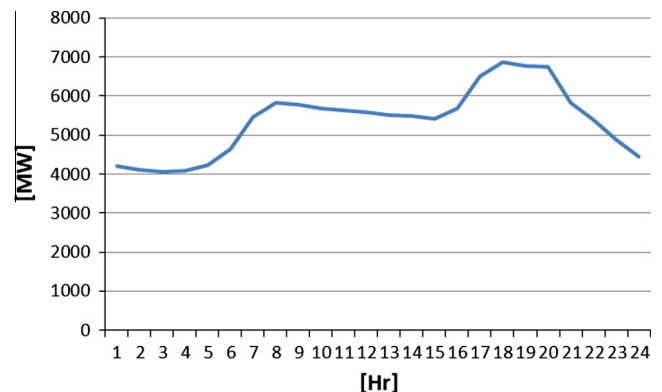


Fig. A.9. Daily load profile.

dispatch results. In this new work, we have attempted to quantify the economic impact, primarily the production cost and market price impacts, of modeling and incorporating different types of DR in a day-ahead electricity market. As a general matter, DR can have significant drag on electricity prices, as evidenced from the results. While this phenomenon helps reduce the load payment, it also has the effect of reduced generator revenue, hence, affecting the social welfare. In this case, generators (suppliers) portion of social welfare was reduced, while consumers, representing DR, portion of social welfare was increased. This outcome would certainly force us to revisit the question of efficient and fair allocation mechanism for a system with varying social welfare due to DR resources.

Appendix A. System data

The following Table A.3 shows the generator offers, used in the simulation of the paper. The following load profile representing 24 h load shape, shown in Fig. A.9, was also used in the simulation.

References

- [1] FERC. Federal energy regulatory commission report to congress: implementation proposal for the national action plan on demand response; 2011. <<http://www.ferc.gov>>.
- [2] Kowli A, Gross G. Quantifying the variable effects of systems with demand response resources. In: 2010 IREP symposium-bulk power system dynamics and control VIII; 1–6 August 2010. p. 1–10.
- [3] Strbac G, D Farmer E, Cory BJ. Framework for the incorporation of demand-side in a competitive electricity market. *IEE Proc Gener Transm Distrib* 1996;143(3):232–7.
- [4] Jonghe CD, Hobbs B, Belmans R. Optimal generation mix with short term demand response and wind penetration. *IEEE Trans Power Syst* 2012;27(2):830–9.
- [5] Lee H, Wilkins CL. A practical approach to appliance load control analysis: a water heater case study. *IEEE Trans Power Appl Syst* 1983;PAS-102.
- [6] Ng K, Sheble G. Direct load control-A profit based load management using linear programming. *IEEE Trans Power Syst* 1998;13(2):688–94.
- [7] Kurucz CN, Brandt D, Sim S. A linear programming model for reducing system peak through customer load control programs. *IEEE Trans Power Syst* 1996;11(4):1817–24.
- [8] Popovic Z. Determination of optimal direct load control strategy using linear programming. In: 15th International conference and exhibition on electricity distribution, Proc Cired, Nice; 1–4 June 1999.
- [9] Cohen A, Wang C. An optimization method for load management scheduling. *IEEE Trans Power Syst* 1988;3(2):612–8.
- [10] Chu W, Chen B, Fu C. Scheduling of direct load control to minimize load reduction for a utility suffering from generation shortage. *IEEE Trans Power Syst* 1993;8(4):1525–30.
- [11] Madaeni SH, Sioshansi R. Using demand response to improve the emission benefits of wind. *IEEE Trans Power Syst* 2013;28(2):1385–94.
- [12] Wu L. Impact of price-based demand response on market clearing and locational marginal prices. *IET Gener Transm Distrib* 2013;7(10):1087–95.
- [13] Rahmani-andebili M. Investigating effects of responsive loads models on unit commitment collaborated with demand-side resources. *IET Gener Transm Distrib* 2013;7(4):420–30.
- [14] Wang Q, Wang J, Guan Y. Stochastic unit commitment with uncertain demand response. *IEEE Trans Power Syst* 2013;28(1):562–3.
- [15] Sahebi MMR, Hosseini SH. Stochastic security constrained unit commitment incorporating demand side reserve. *Int J Electr Power Energy Syst* 2014;56:175–84.
- [16] Arasteh HR, Parsa Moghaddam M, Sheikh-El-Eslami MK, Abdollahi A. Integrating commercial demand response resources with unit commitment. *Int J Electr Power Energy Syst* 2013;51(1):153–61.
- [17] Washington U. Power systems test case archive IEEE 118 bus system; 1993. <<http://www.ee.washington.edu/research/pstca/pf118/pgtca118bus.htm>>.
- [18] NERC. North American electric reliability corporation report on data collection for demand-side management for quantifying its influence on reliability: results and recommendations, Princeton, NJ; December 2007.
- [19] Viana A, Pedroso JP. A new MILP-based approach for unit commitment in power production planning. *Int J Electr Power Energy Syst* 2013;44(1):997–1005.
- [20] Bisanovic S, Hajro M, Dlakic M. Unit commitment problem in deregulated environment. *Int J Electr Power Energy Syst* 2012;42(1):150–7.
- [21] Rajan D, Takriti S. Minimum up/down polytopes of the UC problem with start-up costs. IBM, research report RC23628; June 2005.
- [22] Pinto H, Magnago F, Brignone S, Alsac O, Stott B. Security constrained unit commitment: network modeling and solution issues. In: Power systems conference and exposition, IEEE PES; October 29–November 1, 2006. p. 1759–66.
- [23] Conejo AJ, Castillo E, Minguez R, Garcia-Bertrand R. Decomposition techniques in mathematical programming: engineering and science applications. Berlin: Springer-Verlag; 2006.
- [24] Alemany J, Magnago F. Benders decomposition applied to security constrained unit commitment: initialization of the algorithm. *Int J Electr Power Energy Syst* 2015;66(3):53–66.